

Q1 :

Find the coordinates of the point which divides the line segment joining the points (-2, 3, 5) and (1, -4, 6) in the ratio (i) 2:3 internally, (ii) 2:3 externally.

Answer :

(i) The coordinates of point R that divides the line segment joining points P ( $x_1, y_1, z_1$ ) and Q ( $x_2, y_2, z_2$ ) internally in the ratio  $m: n$  are

$$\left( \frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n}, \frac{mz_2 + nz_1}{m+n} \right)$$

Let R ( $x, y, z$ ) be the point that divides the line segment joining points (-2, 3, 5) and (1, -4, 6) internally in the ratio 2:3

$$x = \frac{2(1) + 3(-2)}{2+3}, y = \frac{2(-4) + 3(3)}{2+3}, \text{ and } z = \frac{2(6) + 3(5)}{2+3}$$

$$\text{i.e., } x = \frac{-4}{5}, y = \frac{1}{5}, \text{ and } z = \frac{27}{5}$$

Thus, the coordinates of the required point are  $\left( \frac{-4}{5}, \frac{1}{5}, \frac{27}{5} \right)$ .

(ii) The coordinates of point R that divides the line segment joining points P ( $x_1, y_1, z_1$ ) and Q ( $x_2, y_2, z_2$ ) externally in the ratio  $m: n$  are

$$\left( \frac{mx_2 - nx_1}{m-n}, \frac{my_2 - ny_1}{m-n}, \frac{mz_2 - nz_1}{m-n} \right)$$

Let R ( $x, y, z$ ) be the point that divides the line segment joining points (-2, 3, 5) and (1, -4, 6) externally in the ratio 2:3

$$x = \frac{2(1) - 3(-2)}{2-3}, y = \frac{2(-4) - 3(3)}{2-3}, \text{ and } z = \frac{2(6) - 3(5)}{2-3}$$

$$\text{i.e., } x = -8, y = 17, \text{ and } z = 3$$

Thus, the coordinates of the required point are (-8, 17, 3).

Q2 :

Given that P (3, 2, -4), Q (5, 4, -6) and R (9, 8, -10) are collinear. Find the ratio in which Q divides PR.

**Answer :**

Let point Q (5, 4, -6) divide the line segment joining points P (3, 2, -4) and R (9, 8, -10) in the ratio  $k:1$ .

Therefore, by section formula,

$$(5, 4, -6) = \left( \frac{k(9)+3}{k+1}, \frac{k(8)+2}{k+1}, \frac{k(-10)-4}{k+1} \right)$$

$$\Rightarrow \frac{9k+3}{k+1} = 5$$

$$\Rightarrow 9k+3 = 5k+5$$

$$\Rightarrow 4k = 2$$

$$\Rightarrow k = \frac{2}{4} = \frac{1}{2}$$

Thus, point Q divides PR in the ratio 1:2.

**Q3 :**

Find the ratio in which the YZ-plane divides the line segment formed by joining the points (-2, 4, 7) and (3, -5, 8).

**Answer :**

Let the YZ plane divide the line segment joining points (-2, 4, 7) and (3, -5, 8) in the ratio  $k:1$ .

Hence, by section formula, the coordinates of point of intersection are given by

$$\left( \frac{k(3)-2}{k+1}, \frac{k(-5)+4}{k+1}, \frac{k(8)+7}{k+1} \right)$$

On the YZ plane, the x-coordinate of any point is zero.

$$\frac{3k-2}{k+1} = 0$$

$$\Rightarrow 3k-2 = 0$$

$$\Rightarrow k = \frac{2}{3}$$

Thus, the YZ plane divides the line segment formed by joining the given points in the ratio 2:3.

**Q4 :**

Using section formula, show that the points A (2, -3, 4), B (-1, 2, 1) and  $C\left(0, \frac{1}{3}, 2\right)$  are collinear.

**Answer :**

The given points are A (2, -3, 4), B (-1, 2, 1), and  $C\left(0, \frac{1}{3}, 2\right)$ .

Let P be a point that divides AB in the ratio  $k:1$ .

Hence, by section formula, the coordinates of P are given by

$$\left(\frac{k(-1)+2}{k+1}, \frac{k(2)-3}{k+1}, \frac{k(1)+4}{k+1}\right)$$

Now, we find the value of  $k$  at which point P coincides with point C.

By taking  $\frac{-k+2}{k+1} = 0$ , we obtain  $k = 2$ .

For  $k = 2$ , the coordinates of point P are  $\left(0, \frac{1}{3}, 2\right)$ .

i.e.,  $C\left(0, \frac{1}{3}, 2\right)$  is a point that divides AB externally in the ratio 2:1 and is the same as point P.

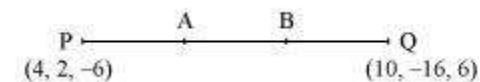
Hence, points A, B, and C are collinear.

**Q5 :**

Find the coordinates of the points which trisect the line segment joining the points P (4, 2, -6) and Q (10, -16, 6).

**Answer :**

Let A and B be the points that trisect the line segment joining points P (4, 2, -6) and Q (10, -16, 6)



Point A divides PQ in the ratio 1:2. Therefore, by section formula, the coordinates of point A are given by

$$\left(\frac{1(10)+2(4)}{1+2}, \frac{1(-16)+2(2)}{1+2}, \frac{1(6)+2(-6)}{1+2}\right) = (6, -4, -2)$$

Point B divides PQ in the ratio 2:1. Therefore, by section formula, the coordinates of point B are given by

$$\left( \frac{2(10)+1(4)}{2+1}, \frac{2(-16)+1(2)}{2+1}, \frac{2(6)-1(6)}{2+1} \right) = (8, -10, 2)$$

Thus,  $(6, -4, -2)$  and  $(8, -10, 2)$  are the points that trisect the line segment joining points P  $(4, 2, -6)$  and Q  $(10, -16, 6)$ .

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