NCERT Solutions Class 11 Maths Chapter 10 Exercise 10.3

Ouestion 1:

Reduce the following equation into slope-intercept form and find their slopes and the yintercepts.

(ii) 6x + 3y - 5 = 0(i) x + 7y = 0(iii) y=0

Solution:

The given equation is x + 7y = 0(i) It can be written as

$$y = -\frac{1}{7}x + 0$$

This equation is of the form y = mx + c, where $m = -\frac{1}{7}$ and c = 0

Therefore, equation x + 7y = 0 is the slope-intercept form, where the slope and the y-DOM:5 HINCH OWDIN

intercept are $\overline{7}$ and 0 respectively.

The given equation is 6x + 3y - 5 = 0(ii) It can be written as

$$y = \frac{1}{3} \left(-6x + 5 \right)$$

 $y = -2x + \frac{5}{3}$

This equation is of the form y = mx + c, where m = -2 and $c = \frac{5}{3}$. Therefore, equation 6x+3y-5=0 is the slope-intercept form, where the slope and the y-

intercept are -2 and $\overline{3}$ respectively.

(iii) The given equation is y = 0. It can be written as y = 0.x + 0

This equation is of the form y = mx + c, where m = 0 and c = 0.

Therefore, equation y=0 is in the slope-intercept form, where the slope and the yintercept are 0 and 0 respectively.

Question 2:

Reduce the following equations into intercept form and find their intercepts on the axis.

(i) 3x+2y-12=0 (ii) 4x-3y=6(iii) 3y + 2 = 0

Solution:

(i) The given equation is 3x+2y-12=0It can be written as

$$3x + 2y = 12$$

$$\frac{3x}{12} + \frac{2y}{12} = 1$$

$$\frac{x}{4} + \frac{y}{6} = 1$$
 ...(1)

$$x = y$$

This equation is of the form $\frac{a}{a} + \frac{b}{b} = 1$, where a = 4 and b = 6.

Therefore, equation (1) is in the intercept form, where the intercepts on the x and y axes are 4 and 6 respectively.

(ii) The given equation is 4x-3y=6. It can be written as

> $\frac{4x}{6} - \frac{3y}{6} = 1$ $\frac{2x}{3} - \frac{y}{2} = 1$ $\frac{x}{3} + \frac{y}{(-2)} = 1 \qquad \dots (2)$

This equation is of the form $a^{-+}b^{--}$, where $a^{-}2$ and b = -2. Therefore, equation (2) is in the intercept form, where the intercepts on x and y-axes are

- $\overline{2}$ and -2 respectively.
- (iii) The given equation is 3y+2=0It can be written as

$$3y = -2$$

$$\frac{y}{\left(-\frac{2}{3}\right)} = 1 \qquad \dots(3)$$

This equation is of the form $\frac{x}{a} + \frac{y}{b} = 1$, where a = 0 and $b = -\frac{2}{3}$.

Therefore, equation (3) is in the intercept form, where the intercepts on the y-axis is $\overline{3}$ and it has no intercept on the x-axis.

2

Question 3:

Reduce the following equations into normal form. Find their perpendicular distance from the origin and angle between perpendicular and the positive x-axis.

(i)
$$x - 3\sqrt{y} + 8 = 0$$
 (ii) $y - 2 = 0$ (iii) $x - y = 4$

Solution:

The given equation is $x - 3\sqrt{y} + 8 = 0$ (i) It can be written as

$$x - 3\sqrt{y} = -8$$
$$-x + 3\sqrt{y} = 8$$

On dividing both sides by $\sqrt{(-1)^2 + (\sqrt{3})^2} = \sqrt{4} = 2$, we obtain

$$-\frac{x}{2} + \frac{\sqrt{3}}{2}y = \frac{8}{2}$$
$$\left(-\frac{1}{2}\right)x + \left(\frac{\sqrt{3}}{2}\right)y = 4$$
$$x\cos 120^\circ + y\sin 120^\circ = 4$$

Equation (1) is in the normal form.

On comparing equation (1) with the normal form of equation of the line

 $x\cos\omega + y\sin\omega = p$, we obtain $\omega = 120^{\circ}$ and p = 4.

Thus, the perpendicular distance of the line from the origin is 4, while the angle between the perpendicular and the positive x-axis is 120° .

The given equation is y - 2 = 0(ii) It can be represented as 0.x+1.y=2

On dividing both sides by $\sqrt{0^2 + 1^2} = 1$, we obtain

$$0.x + 1.y = 2$$

$$\Rightarrow x \cos 90^\circ + y \sin 90^\circ = 2 \qquad \dots (2)$$

Equation (2) is in the normal form.

On comparing equation (2) with the normal form of equation of line

 $x\cos\omega + y\sin\omega = p$, we obtain $\omega = 90^{\circ}$ and p = 2.

Thus, the perpendicular distance of the line from the origin is 2, while the angle between the perpendicular and the positive *x*-axis is 90° .

(iii) The given equation is x - y = 4. It can be reduced as $1 \cdot x + (-1)y = 4$

> On dividing both sides by $\sqrt{1^2 + (-1)^2} = \sqrt{2}$, we obtain $\frac{1}{\sqrt{2}}x + \left(-\frac{1}{\sqrt{2}}\right)y = \frac{4}{\sqrt{2}}$ $\Rightarrow x \cos\left(2\pi - \frac{\pi}{4}\right) + y \sin\left(2\pi - \frac{\pi}{4}\right) = 2\sqrt{2}$ $\Rightarrow x \cos 315^\circ + y \sin 315^\circ = 2\sqrt{2}$...(3)

Equation (3) is in the normal form.

On comparing equation (3) with the normal form of the equation of the line

 $x\cos\omega + y\sin\omega = p$, we obtain $\omega = 315^\circ$ and $p = 2\sqrt{2}$.

Thus, the perpendicular distance of the line from the origin is $2\sqrt{2}$, while the angle between the perpendicular and the positive x-axis is 315°.

Question 4:

Find the distance of the points (-1,1) from the line 12(x+6) = 5(y-2).

Solution:

The given equation of the line is 12(x+6) = 5(y-2) $\Rightarrow 12x + 72 = 5y - 10$ $\Rightarrow 12x - 5y + 82 = 0$...(1)

On comparing equation (1) with general equation of line Ax + By + C = 0 we obtain A = 12, B = -5 and C = 82.

It is known that the perpendicular distance (d) of a line Ax + By + C = 0 from a point

 (x_1, y_1) is given by $d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$

The given point is $(x_1, y_1) = (-1, 1)$.

Therefore, the distance of point (-1,1) from the given line is

$$\frac{12(-1) + (-5)(1) + 82}{\sqrt{12^2 + (-5)^2}} = \frac{|-12 - 5 + 82|}{\sqrt{169}}$$
$$= \frac{|65|}{13}$$
$$= 5$$

Hence, the distance of point (-1,1) from the given line is 5 units.

Question 5:

Find the points on the x-axis whose distance from the line $3^{+}4^{-}$ are 4 units.

Solution:

The given equation of line is

 $\frac{x}{3} + \frac{y}{4} = 1$ 4x+3y-12 = 0(1)

On comparing equation (1) with general equation of line Ax + By + C = 0 we obtain A = 4, B = 3, and C = -12.

Let (a,0) be the point on the x-axis whose distance from the given line is 4 units.

It is known that the perpendicular distance (d) of a line Ax + By + C = 0 from a point

 (x_1, y_1) is given by $d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$ Therefore,

$$\Rightarrow (4a-12) = 20 \text{ or } -(4a-12) = 20$$

$$\Rightarrow 4a = 20+12 \text{ or } 4a = -20+12$$

$$\Rightarrow a = 8 \text{ or } a = -2$$

Thus, the required points on x-axis are (-2,0) and (8,0).

Question 6:

Find the distance between parallel lines

- 15x+8y-34=0 and 15x+8y+31=0(i)
- l(x+y) + p = 0 and l(x+y) r = 0(ii)

Solution:

It is known that the distance (d) between parallel lines $Ax + By + C_1 = 0$ and $Ax + By + C_2 = 0$ is

given by $d = \frac{\left|C_1 - C_2\right|}{\sqrt{A^2 + B^2}}$

The given parallel lines are 15x+8y-34=0 and 15x+8y+31=0Here, A=15, B=8, $C_1=-34$ and $C_2=-31$ Therefore, the distance between the parallel lines is (i)

$$d = \frac{|C_1 - C_2|}{\sqrt{A^2 + B^2}}$$

= $\frac{|34 - 31|}{\sqrt{(15)^2 + (8)^2}}$ units
= $\frac{|-65|}{\sqrt{289}}$ units
= $\frac{65}{17}$ units

The given parallel lines are l(x+y)+p=0 and l(x+y)-r=0(ii) Here, A = B = l, $C_1 = p$ and $C_2 = -r$ Therefore, the distance between the parallel lines is

$$d = \frac{|C_1 - C_2|}{\sqrt{A^2 + B^2}}$$
$$= \frac{|p+r|}{\sqrt{l^2 + l^2}} units$$
$$= \frac{|p+r|}{\sqrt{2l^2}} units$$
$$= \frac{|p+r|}{l\sqrt{2}} units$$
$$= \frac{1}{\sqrt{2}} \frac{|p+r|}{l} units$$

Question7:

Find equation of the line parallel to the line 3x - 4y + 2 = 0 and passing through the point (-2,3) ADALES ALISCH OWONY

Solution: The equation of the given line is 3x - 4y + 2 = 0 $y = \frac{3x}{4} + \frac{2}{4}$ $y = \frac{3}{4}x + \frac{2}{4}$, which is of the form y = mx + c

Therefore, slope of the given line is $\frac{3}{4}$. It is known that It is known that parallel lines have the same slope.

Slope of the other line is m = 1

Now, the equation of the line that has a slope of $\frac{3}{4}$ and passes through the points (-2,3) is

$$(y-3) = \frac{3}{4} \{x - (-2)\}\$$

$$4y - 12 = 3x + 6\$$

$$3x - 4y + 18 = 0$$

Question 8:

Find the equation of the line perpendicular to the line x-7y+5=0 and having x intercept 3.

Solution:

The given equation of the line is x - 7y + 5 = 0Or $y = \frac{1}{7}x + \frac{5}{7}$, which is of the form y = mx + cTherefore, slope of the given line is $\overline{7}$

$$m = -\frac{1}{\left(\frac{1}{7}\right)} = -7$$

The slope of the line perpendicular to the line having a slope is
The equation of the line with slope -7 and *x*-intercept 3 is given by

$$y = m(x-d)$$

$$y = -7(x-3)$$

$$y = -7x+21$$

$$7x + y - 21 = 0$$

Hence, the required equation of the line is 7x + y - 21 = 0

Find the angles between the lines $\sqrt{3}x + y = 1$ and $x + \sqrt{3}y = 1$ Solution: The given ¹:

The given lines are $\sqrt{3}x + y = 1$ and $x + \sqrt{3}y = 1$

$$y = -\sqrt{3}x + 1$$
 ...(1) and $y = -\frac{1}{\sqrt{3}}x + \frac{1}{\sqrt{3}}$...(2)

The slope of line (1) is $m_1 = -3$, while the slope of the line (2) is $m_2 = -\frac{1}{\sqrt{3}}$

The actual angle i.e., θ between the two lines is given by

$$\begin{aligned}
\Theta(\mathbf{a}\mathbf{n}) &= \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right| \\
&= \left| \frac{-\sqrt{3} + \frac{1}{\sqrt{3}}}{1 + \left(-\sqrt{3} \left(-\frac{1}{\sqrt{3}} \right) \right)} \right| \\
&= \left| \frac{\frac{-3 + 1}{\sqrt{3}}}{1 + 1} \right| = \left| \frac{-2}{2 \times \sqrt{3}} \right| \\
\Theta(\mathbf{a}\mathbf{n}) &= \frac{1}{\sqrt{3}} \\
&\Theta(\mathbf{a}) = 30^\circ
\end{aligned}$$

Thus, the angle between the given lines is either 30° or $180^{\circ} - 30^{\circ} = 150^{\circ}$.

Question 10:

The line through the points (h,3) and (4,1) intersects the line 7x-9y-19=0. At right angle. Find the value of *h*.

Solution:

The slope of the line passing through points (h,3) and (4,1) is

$$m_1 = \frac{1-3}{4-h} = \frac{-2}{4-h}$$

 $-\frac{19}{9}$ is $m_2 = \frac{7}{9}$ The slope of the line 7x - 9y - 19 = 0 or 9 It is given that the two lines are perpendicular Therefore,

$$\Rightarrow m_1 \times m_2 = -1$$

$$\Rightarrow \frac{-14}{36 - 9h} = -1$$

$$\Rightarrow 14 = 36 - 9h$$

$$\Rightarrow 9h = 36 - 14$$

$$\Rightarrow h = \frac{22}{9}$$

Thus, the value of $h = \frac{22}{9}$.

Question 11:

Prove that the line through the point (x_1, y_1) and parallel to the line Ax + By + C = 0 is $A(x-x_1) + B(y-y_1) = 0$

Solution:

The slope of line Ax + By + C = 0 or $y = \left(-\frac{A}{B}\right)x + \left(-\frac{C}{B}\right)$ is $m = -\frac{A}{B}$ It is known that parallel lines have the same slope.

Therefore, slope of the other line $= m = -\frac{A}{B}$

The equation of the line passing through point (x_1, y_1) and having slope $m = -\frac{A}{B}$ is

$$y - y_{1} = m(x - x_{1})$$

$$y - y_{1} = -\frac{A}{B}(x - x_{1})$$

$$B(y - y_{1}) = -A(x - x_{1})$$

$$A(x - x_{1}) + B(y - y_{1}) = 0$$

Hence, the line through point (x_1, y_1) and parallel to line Ax + By + C = 0 is $A(x-x_1) + B(y-y_1) = 0$

Question 12:

Two lines passing through the points (2,3) intersects each other at an angle of 60°. If slope of one line is 2, find equation of the other line.

Solution:

It is given that the slope of the first line, $m_1 = 2$.

Let the slope of the other line be m_2 .

The angle between the two lines is 60° .

$$\begin{aligned} & \operatorname{en} \quad = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right| \\ & \tan 60^\circ = \left| \frac{2 - m_2}{1 + 2m_2} \right| \\ & \sqrt{3} = \pm \left(\frac{2 - m_2}{1 + 2m_2} \right) \end{aligned}$$

$$\sqrt{3} = \left(\frac{2 - m_2}{1 + 2m_2}\right) \qquad \sqrt{3} = -\left(\frac{2 - m_2}{1 + 2m_2}\right)$$
$$\sqrt{3} (1 + 2m_2) = 2 - m_2 \qquad \sqrt{3} (1 + 2m_2) = -(2 - m_2)$$
$$\sqrt{3} + 2\sqrt{3}m_2 + m_2 = 2 \qquad \sqrt{3} + 2\sqrt{3}m_2 - m_2 = -2$$
$$\sqrt{3} + (2\sqrt{3} + 1)m_2 = 2 \qquad \sqrt{3} + (2\sqrt{3} - 1)m_2 = -2$$
$$m_2 = \frac{2 - \sqrt{3}}{(2\sqrt{3} + 1)} \qquad \text{or} \qquad m_2 = \frac{-(2 + \sqrt{3})}{(2\sqrt{3} - 1)}$$

<u>Case 1</u>:

 $m_2 = \frac{2 - \sqrt{3}}{\left(2\sqrt{3} + 1\right)}$

The equation of the line passing through the point (2,3) and having a slope of $\frac{2-\sqrt{3}}{(2\sqrt{3}+1)}$ is $(\nu-3) = \frac{2-\sqrt{3}}{(2\sqrt{3}+1)}$ ($\nu-2$)

$$(y-3) = \frac{2-\sqrt{3}}{(2\sqrt{3}+1)}(x-2)$$

(2\sqrt{3}+1)y-3(2\sqrt{3}+1) = (2-\sqrt{3})x-2(2-\sqrt{3})
(\sqrt{3}-2)x+(2\sqrt{3}+1)y = -1+8\sqrt{3}

In this case, the equation of the other line is $(\sqrt{3}-2)x + (2\sqrt{3}+1)y = -1 + 8\sqrt{3}$ Case 2: $m_2 = \frac{-(2+\sqrt{3})}{(2\sqrt{3}-1)}$

$$m_2 = \frac{-\left(2+\sqrt{3}\right)}{\left(2\sqrt{3}-1\right)}$$

The equation of the line passing through the point (2,3) and having a slope of $\frac{-(2+\sqrt{3})}{(2\sqrt{3}-1)}$ is $-(2+\sqrt{2})$

$$(y-3) = \frac{-(2+\sqrt{3})}{(2\sqrt{3}-1)}(x-2)$$

(2\sqrt{3}-1)y-3(2\sqrt{3}-1) = -(2-\sqrt{3})x+2(2-\sqrt{3})
(2-\sqrt{3})x+(2\sqrt{3}-1)y = 4-2\sqrt{3}+6\sqrt{3}-3
(2-\sqrt{3})x+(2\sqrt{3}-1)y = 1+8\sqrt{3}

If the case of the equation of the other line is $(2-\sqrt{3})x + (2\sqrt{3}-1)y = 1 + 8\sqrt{3}$

Thus, the required equation of the other line is $(\sqrt{3}-2)x+(2\sqrt{3}+1)y=-1+8\sqrt{3}$ $(2-\sqrt{3})x+(2\sqrt{3}-1)y=1+8\sqrt{3}$

Question 13:

Find the equation of the right bisector of the line segment joining the points (3,4) and (-1,2).

Solution:

The right bisector of a line segment bisects the line segment at 90°.

The end points of the line segment are given as A(3,4) and B(-1,2)Accordingly, mid-point of $AB = \left(\frac{3-1}{2}, \frac{4+2}{0}\right) = (1,3)$ Minck amai Slope of $AB = \frac{2-4}{-1-3} = \frac{-2}{-4} = \frac{1}{2}$ AB = -Slope of the line perpendicular to The equation of the line passing through (1,3) and having a slope of -2 is (y-3) = -2(x-1)y - 3 = -2x + 22x + v = 5

Thus, the required equation of the line is 2x + y = 5.

Question 14:

Find the coordinates of the foot of perpendicular from the points (-1,3) to the line 3x - 4y - 16 = 0.

Solution:

Let (a,b) be the coordinates of the foot of the perpendicular from the points (-1,3) to the line 3x - 4y - 16 = 0

$$a_{1} = \frac{(a, b)}{3x - 4y - 16 = 0}$$

Slope of the line joining (-1,3) and (a,b), $m_{1} = \frac{b-3}{a+1}$
Slope of the line $3x - 4y - 16 = 0$ or $y = \frac{3}{4}x - 4$, $m_{2} = \frac{3}{4}$
Since these two lines are perpendicular, $m_{1} \times m_{2} = -1$
Therefore,
$$= \frac{(b-3)}{4a+4} = -1$$
$$= \frac{3b-9}{4a+4} = -1$$
$$= \frac{3a-4b}{2} = -1$$
$$= \frac{1}{2}$$
$$= \frac{1}{2}$$
$$= \frac{1}{2}$$
Thus, the required coordinates of the foot of the perpendicular are $\left(\frac{68}{25}, \frac{49}{25}\right)$

Question 15:

The perpendicular from the origin to the line y = mx + c meets it at the a point (-1, 2). Find the values of *m* and *c*.

Solution:

The given equation of line is y = mx + c

It is given that the perpendicular from the origin meets the given line at (-1,2).

Therefore, the line joining the points (0,0) and (-1,2) is perpendicular to the given line

Slope of the line joining (0,0) and (-1,2) is $\frac{2}{-1} = -2$

The slope of the given line is *m* Therefore,

$$m \times (-2) = -1$$
 [The two lines are perpendicular]
 $\Rightarrow m = \frac{1}{2}$

Since points (-1,2) lies on the given line, it satisfies the equation y = mx + cTherefore,

$$\Rightarrow 2 = m(-1) + c$$
$$\Rightarrow 2 = 2 + \frac{1}{2}(-1) + c$$
$$\Rightarrow c = 2 + \frac{1}{2} = \frac{5}{2}$$

Thus, the respective values of m and c are $\frac{1}{2}$ and $\frac{5}{2}$

Question 16:

If p and q are the lengths of perpendicular from the origin to the lines $x\cos\theta - y\sin\theta = k\cos 2\theta$ and $x\sec\theta + y\csc\theta = k$, respectively, prove that $p^2 + 4q^2 = k^2$

Solution:

The equations of given lines are $x \cos \theta - y \sin \theta = k \cos 2\theta$...(1) $x \sec \theta + y \cos ec\theta = k$...(2)

The perpendicular distance(d) of a line Ax + By + C = 0 from a point (x_1, x_2) is given by

$$d = \frac{\left|Ax_1 + By_1 + C\right|}{\sqrt{A^2 + B^2}}$$

On comparing equation(1) to the general equation of a line i.e., Ax + By + C = 0, we obtain $A = \cos\theta$, $B = -\sin\theta$ and $C = -k\cos 2\theta$

It is given that p is the length of the perpendicular from (0,0) to line (1).

Therefore,
$$p = \frac{|A(0) + B(0) + C|}{\sqrt{A^2 + B^2}} = \frac{|C|}{\sqrt{A^2 + B^2}} = \frac{|-k\cos 2\theta|}{\sqrt{\cos^2 \theta + \sin^2 \theta}} = |-k\cos 2\theta| \qquad \dots(3)$$

On comparing equation (2) to the general equation of line i.e., Ax + By + C = 0, we obtain $A = \sec \theta, B = \csc \theta$ and C = -k

It is given that q is the length of the perpendicular from (0,0) to line (2)

Therefore, $p = \frac{|A(0) + B(0) + C|}{\sqrt{A^2 + B^2}} = \frac{|C|}{\sqrt{A^2 + B^2}} = \frac{|-k|}{\sqrt{\sec^2 \theta + \cos ec^2 \theta}} \dots (4)$

From (3) and (4), we have

$$p^{2} + 4q^{2} = \left(\left|-k\cos 2\theta\right|\right)^{2} + 4\left(\frac{\left|-k\right|}{\sqrt{\sec^{2}\theta + \csc ec^{2}\theta}}\right)^{2}$$

$$= k^{2}\cos^{2}2\theta + \frac{4k^{2}}{\left(\sec^{2}\theta + \csc ec^{2}\theta\right)}$$

$$= k^{2}\cos^{2}2\theta + \frac{4k^{2}}{\left(\frac{1}{\cos^{2}\theta} + \frac{1}{\sin^{2}\theta}\right)}$$

$$= k^{2}\cos^{2}2\theta + \left(\frac{4k^{2}}{\frac{\sin^{2}\theta + \cos^{2}\theta}{\sin^{2}\theta \cos^{2}\theta}}\right)$$

$$= k^{2}\cos^{2}2\theta + \left(\frac{4k^{2}}{\frac{1}{\sin^{2}\theta \cos^{2}\theta}}\right)$$

$$= k^{2}\cos^{2}2\theta + k^{2}(\sin\theta \cos\theta)^{2}$$

$$= k^{2}(\cos^{2}2\theta + k^{2}\sin^{2}2\theta)$$

$$= k^{2}\left((\cos^{2}2\theta + \sin^{2}2\theta)\right)$$

$$= k^{2}$$

Hence, we proved that $p^2 + 4q^2 = k^2$ Ouestion 17:

In the triangle ABC with vertices A(2,3), B(4,-1) and C(1,2), find the equation and length of altitude from the vertex A.

Solution:

Let AD be the altitude of triangle ABC from vertex A. Accordingly, $AD \perp BC$

The equation of the line passing through point (2,3) and having a slope of 1 is

$$\Rightarrow (y-3) = 1(x-2)$$
$$\Rightarrow x - y + 1 = 0$$
$$\Rightarrow y - x = 1$$

Therefore, equation of the altitude from vertex A = y - x = 1

Length of AD = Length of the perpendicular from A(2,3) to BC The equation of BC is

$$\Rightarrow (y+1) = \frac{2+1}{1-4}(x-4)$$
$$\Rightarrow (y+1) = -1(x-4)$$
$$\Rightarrow y+1 = -x+4$$
$$\Rightarrow x+y-3 = 0 \qquad \dots (1)$$

The perpendicular distance (d) of a line Ax + By + C = 0 from a point (x_1, y_1) is given by

$$d = \frac{\left|Ax_1 + By_1 + C\right|}{\sqrt{A^2 + B^2}}$$

On comparing equation (1) to the general equation of line Ax + By + C = 0, we obtain A = 1, B = 1 and C = 3.

$$AD = \frac{|1 \times 2 + 1 \times 3 - 3|}{\sqrt{1^2 + 1^2}} = \frac{2}{\sqrt{2}} = \sqrt{2}un$$

Length of

Thus, the equation and length of the altitude from vertex A are y - x = 1 and $\sqrt{2}$ units.

Question 18:

If p is the length of perpendicular from the origin to the line whose intercepts on the x-axis are a and b, then show that $\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$

Solution:

It is known that the equation of a line whose intercepts on the axis a and b is

 $\frac{x}{a} + \frac{y}{b} = 1$ bx + ay = ab $bx + ay - ab = 0 \qquad \dots (1)$

The perpendicular distance (d) of a line Ax + By + C = 0 from a point (x_1, y_1) is given by

$$d = \frac{\left|Ax_1 + By_1 + C\right|}{\sqrt{A^2 + B^2}}$$

On comparing equation (1) to the general equation of line Ax+By+C=0, we obtain A=b, B=a and C=-ab.

Therefore, if p is the length of the perpendicular from point $(x_1, y_1) = (0, 0)$ to line (1), We obtain

$$p = \frac{\left|A(0) + B(0) - ab\right|}{\sqrt{a^2 + b^2}}$$
$$= \frac{\left|-ab\right|}{\sqrt{a^2 + b^2}}$$
both sides, we obtain

On squaring both sides, we obtain

