

# RD Sharma

## Solutions

### Class 11 Maths

#### Chapter 19

#### Ex 19.4

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Same textbooks, klack away

### Arithmetic Progressions Ex 19.4 Q1

(i) 50, 46, 42, ..., 10 terms

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{10} = \frac{10}{2} [2 \times 50 + (10-1)(-4)] \\ = 320$$

(ii) 13, 5, ..., 12 terms

$$S_{12} = \frac{12}{2} [2 \times 13 + (12-1)(-8)] \\ = 6 \times 24 = 144$$

(iii)  $3, \frac{9}{2}, 6, \frac{15}{2}, \dots, 25$  terms

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{25} = \frac{25}{2} \left( 2 \times 3 + 24 \times \frac{3}{2} \right) \\ = 525$$

(iv) 41, 36, 31, ..., 12 terms

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{12} = \frac{12}{2} [2 \times 41 + (11)(-5)] \\ = 162$$

(v)  $a+b, a-b, a-3b, \dots$  to 22 terms

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{22} = \frac{22}{2} [2a + 21(-2b)] \\ = 22a - 440b$$

(vi)  $(x-y)^2, (x^2+y^2), (x+y)^2, \dots, x$  terms

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$= \frac{n}{2} [2(x^2+y^2-2xy) + (n-1)(-2xy)]$$

$$= n[(x-y)^2 + (n-1)xy]$$

$\frac{x-y}{x+y}, \frac{3x-2y}{x+y}, \frac{5x-3y}{x+y}, \dots$  to  $n$  terms

$n$ th term in above sequence is  $\frac{(2n-1)x - ny}{x+y}$

Sum of  $n$  terms is given by

$$\frac{1}{x+y} [x + 3x + 5x + \dots + (2n-1)x - (y + 2y + 3y + \dots + ny)]$$

$$= \frac{1}{x+y} \left[ \frac{n}{2} (2x + (n-1)2x) - \frac{n(n+1)y}{2} \right]$$

$$= \frac{1}{2(x+y)} [2n^2x - 2n^2y - ny]$$

### Arithmetic Progressions Ex 19.4 Q2

(i)  $2 + 5 + 8 + \dots + 182.$

$a_n$  term of given A.P is 182

$$a_n = a + (n - 1)d = 182$$

$$\Rightarrow 182 = 2 + (n - 1)3$$

or  $n = 61$

Then,

$$\begin{aligned} S_n &= \frac{n}{2}[a + l] \\ &= \frac{61}{2}[2 + 182] \\ &= 61 \times 92 \\ &= 5612 \end{aligned}$$

(ii)  $101 + 99 + 97 + \dots + 47$

$a_n$  term of A.P of  $n$  terms is 47.

$$\therefore 47 = a + (n - 1)d$$

$$47 = 101 + (n - 1)(-2)$$

or  $n = 28$

Then,

$$\begin{aligned} S_n &= \frac{n}{2}[a + l] \\ &= \frac{28}{2}[101 + 47] \\ &= 14 \times 148 \\ &= 2072 \end{aligned}$$

(iii)  $(a - b)^2 + (a^2 + b^2) + (a + b)^2 + \dots + [(a + b)^2 + 6ab]$

Let number of terms be  $n$

Then,

$$a_n = (a + b)^2 + 6ab$$

$$\Rightarrow (a - b)^2 + (n - 1)(2ab) = (a + b)^2 + 6ab$$

$$\Rightarrow a^2 + b^2 - 2ab + 2abn - 2ab = a^2 + b^2 + 2ab + 6ab$$

$$\Rightarrow n = 6$$

Then,

$$\begin{aligned} S_n &= \frac{n}{2}[a + l] \\ S_6 &= \frac{6}{2}[a^2 + b^2 - 2ab + a^2 + b^2 + 2ab + 6ab] \\ &= 6[a^2 + b^2 + 3ab] \end{aligned}$$

### Arithmetic Progressions Ex 19.4 Q3

A.P formed is  $1, 2, 3, 4, \dots, n$ .

Here,

$$a = 1$$

$$d = 1$$

$$l = n$$

$$\begin{aligned}\text{So sum of } n \text{ terms } = S_n &= \frac{n}{2} [2a + (n-1)d] \\ &= \frac{n}{2} [2 + (n-1)1] \\ &= \frac{n(n+1)}{2} \text{ is the sum of first } n \text{ natural numbers.}\end{aligned}$$

#### Arithmetic Progressions Ex 19.4 Q4

The natural numbers which are divisible by 2 or 5 are:

$$2 + 4 + 5 + 6 + 8 + 10 + \dots + 100 = (2 + 4 + 6 + \dots + 100) + (5 + 15 + 25 + \dots + 95)$$
 Now

$(2 + 4 + 6 + \dots + 100)$  and  $(5 + 15 + 25 + \dots + 95)$  are AP with common difference 2 and 10 respectively.

Therefore

$$\begin{aligned}2 + 4 + 6 + \dots + 100 &= 2 \frac{50}{2} (1 + 50) \\ &= 2550\end{aligned}$$

Again

$$\begin{aligned}5 + 15 + 25 + \dots + 95 &= 5(1 + 3 + 5 + \dots + 19) \\ &= 5 \left( \frac{10}{2} \right) (1 + 19) \\ &= 500\end{aligned}$$

Therefore the sum of the numbers divisible by 2 or 5 is:

$$\begin{aligned}2 + 4 + 5 + 6 + 8 + 10 + \dots + 100 &= 2550 + 500 \\ &= 3050\end{aligned}$$

#### Arithmetic Progressions Ex 19.4 Q5

The series of  $n$  odd natural numbers are  $1, 3, 5, \dots, n$

Where  $n$  is odd natural number

Then, sum of  $n$  terms is

$$\begin{aligned}S_n &= \frac{n}{2} [2a + (n-1)d] \\ &= \frac{n}{2} [2(1) + (n-1)(2)] \\ &= n^2\end{aligned}$$

The sum of  $n$  odd natural numbers is  $n^2$ .

#### Arithmetic Progressions Ex 19.4 Q6

The series so formed is 101, 103, 105, ..., 199

Let number of terms be  $n$

Then,

$$a_n = a + (n - 1)d = 199$$

$$\Rightarrow 199 = 101 + (n - 1)2$$

$$\Rightarrow n = 50$$

The sum of  $n$  terms  $= S_n = \frac{n}{2}[a + l]$

$$\begin{aligned} S_{50} &= \frac{50}{2}[101 + 199] \\ &= 7500 \end{aligned}$$

The sum of odd numbers between 100 and 200 is 7500.

#### Arithmetic Progressions Ex 19.4 Q7

The odd numbers between 1 and 100 divisible by 3 are 3, 9, 15, ..., 999

Let the number of terms be  $n$  then,  $n$ th term is 999.

$$a_n = a + (n - 1)d$$

$$999 = 3 + (n - 1)6$$

$$\Rightarrow n = 167$$

The sum of  $n$  terms

$$S_n = \frac{n}{2}[a + l]$$

$$\Rightarrow S_{167} = \frac{167}{2}[3 + 999]$$

$$= 83667$$

Hence proved.

#### Arithmetic Progressions Ex 19.4 Q8

The required series is 85, 90, 95, ..., 715

Let there be  $n$  terms in the A.P

Then,

$$n\text{th term} = 715$$

$$715 = 85 + (n - 1)5$$

$$n = 127$$

Then,

$$S_n = \frac{n}{2}[a + l]$$

$$S_{127} = \frac{127}{2}[85 + 715]$$

$$= 50800$$

#### Arithmetic Progressions Ex 19.4 Q9

The series of integers divisible by 7 between 50 and 500 are

56, 63, 70, ..., 497

Let the number of terms be  $n$  then,  $n$ th term = 497

$$a_n = a + (n - 1)d$$

$$\Rightarrow 497 = 56 + (n - 1)7$$

$$\Rightarrow n = 64$$

The sum  $S_n = \frac{n}{2}[a + l]$

$$\begin{aligned}\Rightarrow S_{64} &= \frac{64}{2}[56 + 497] \\ &= 32 \times 553 \\ &= 17696\end{aligned}$$

### Arithmetic Progressions Ex 19.4 Q10

All even integers will have common difference = 2

$\therefore$  A.P is 102, 104, 106, ..., 998

$$t_n = a + (n - 1)d$$

$$t_n = 998, a = 102, d = 2$$

$$998 = 102 + (n - 1)(2)$$

$$998 = 102 + 2n - 2$$

$$998 - 100 = 2n$$

$$2n = 898$$

$$n = 449$$

$S_{449}$  can be calculated by

$$S_n = \frac{n}{2}[a + l]$$

$$= \frac{449}{2}[102 + 998]$$

$$= \frac{449}{2} \times 1100$$

$$= 449 \times 550$$

$$= 246950$$

### Arithmetic Progressions Ex 19.4 Q11

The series formed by all the integers between 100 and 550 which are divisible by 9 is

108, 117, 123, ..., 549

Let there be  $n$  terms in the A.P then, the  $n$ th term is 549

$$549 = a + (n - 1)d$$

$$549 = 108 + (n - 1)9$$

$$\Rightarrow n = 50$$

Then,

In the given series  $3 + 5 + 7 + 9 + \dots$  to  $3n$

Here,

$$a = 3$$

$$d = 2$$

$$\text{Number of terms} = 3n$$

The sum of  $n$  term is

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\begin{aligned} \Rightarrow S_{3n} &= \frac{3n}{2} [6 + (3n-1)2] \\ &= 3n(2n+3) \end{aligned}$$

#### Arithmetic Progressions Ex 19.4 Q13

The first number between 100 and 800 which on division by 16 leaves the remainder 7 is 112 and last number is 791.

Thus, the series so formed is  $103, 119, \dots, 791$

Let number of terms be  $n$ , then

$$n\text{th term} = 791$$

Then,

$$a_n = a + (n-1)d$$

$$\Rightarrow 791 = 103 + (n-1)16$$

$$\Rightarrow n = 44$$

Then, sum of all terms of the given series is

$$\begin{aligned} S_{44} &= \frac{44}{2} [103 + 791] \\ &= \frac{44 \times 894}{2} \\ &= 19668 \end{aligned}$$

#### Arithmetic Progressions Ex 19.4 Q14

$$(i) 25 + 22 + 19 + 16 + \dots + x = 115$$

Here, sum of the given series of say  $n$  terms is 115

So, the  $n$ th term =  $x$

Here,  $a = 25$  and  $d = 22 - 25 = -3$

$$\therefore a_n = a + (n - 1)d$$

$$\Rightarrow x = 25 - 3(n - 1)$$

$$\Rightarrow x = 28 - 3n \quad \text{---(i)}$$

The sum of  $n$  terms

$$S_n = \frac{n}{2}[a + l]$$

$$\Rightarrow 115 = \frac{n}{2}[25 + 28 - 3n]$$

$$\Rightarrow 230 = 53n - 3n^2$$

$$\Rightarrow 3n^2 - 53n - 230 = 0$$

$$\Rightarrow 3n^2 - 30n - 23n - 230 = 0$$

$$\Rightarrow n = 10 \text{ or } \frac{23}{3}$$

But  $n$  can't be fraction

$$\therefore n = 10 \quad \text{---(ii)}$$

From (i) and (ii)

$$x = 28 - 3n$$

$$= 28 - 3(10)$$

$$= -2$$

$$x = -2$$



$$(ii) 1 + 4 + 7 + 10 + \dots + x = 590$$

$$\text{Here, } a = 1$$

$$d = 4 - 1 = 3$$

Let there be  $n$  terms so the  $n$ th term =  $x$

$$\Rightarrow x = 1 + (n - 1)3$$

$$\Rightarrow x = 3n - 2$$

$$[\because a_n = a + (n - 1)d]$$

---(i)

and

$$S_n = 590$$

[Given]

$$\Rightarrow \frac{n}{2}[a + l] = 590$$

$$\Rightarrow \frac{n}{2}[1 + 3n - 2] = 590$$

$$[\because l = x = 3n - 2]$$

$$\Rightarrow 3n^2 - n - 1080 = 0$$

$$\Rightarrow 3n^2 - 60n + 59n - 1080 = 0$$

$$\Rightarrow 3n(n - 20) + 59(n - 20) = 0$$

$$\Rightarrow n = 20$$

---(ii)

From (i) and (ii)

$$x = 3n - 2$$

$$= 3(20) - 2$$

$$= 58$$

$$x = 58$$

#### Arithmetic Progressions Ex 19.4 Q15

Sum first  $n$  terms of the given AP is

$$S_n = 3n^2 + 2n$$

$$S_{n-1} = 3(n-1)^2 + 2(n-1)$$

$$a_n = S_n - S_{n-1}$$

$$a_n = 3n^2 + 2n - 3(n-1)^2 - 2(n-1)$$

$$a_n = 6n - 1$$

$$a_r = 6r - 1$$

$r$ th term is  $6r - 1$ .

#### Arithmetic Progressions Ex 19.4 Q16

Given,

$$a_1 = -14 = a + 0d \quad \text{---(i)}$$

$$a_5 = 2 = a + 4d \quad \text{---(ii)}$$

Solving (i) and (ii)

$$a_1 = a = -14 \text{ and } d = 4$$

Let there be  $n$  terms then sum of these  $n$  terms = 40

$$\therefore S_n = \frac{n}{2}[2a + (n-1)d]$$

$$\Rightarrow 40 = \frac{n}{2}[-28 + (n-1)4]$$

$$\Rightarrow 4n^2 - 32n - 80 = 0$$

$$\text{or } n = 10 \text{ or } -2$$

But  $n$  can't be negative

$$\therefore n = 10$$

The given A.P has 10 terms.

#### Arithmetic Progressions Ex 19.4 Q17

Given,

$$a_7 = 10$$

$$S_{14} - S_7 = 17 \quad \text{---(i)}$$

$$\therefore S_{14} = 17 + S_7 = 17 + 10 = 27 \quad \text{---(ii)}$$

From (i) and (ii)

$$S_7 = \frac{7}{2}[2a + (7-1)d] \quad \left[ \text{Using } S_n = \frac{n}{2}[2a + (n-1)d] \right]$$

$$\Rightarrow 10 = 7a + 21d \quad \text{---(iii)}$$

and

$$S_{14} = \frac{14}{2}[2a + 13d]$$

$$\Rightarrow 27 = 28a + 182d \quad \text{---(iv)}$$

Solving (iii) and (iv)

$$a = 1 \text{ and } d = \frac{1}{7}$$

$\therefore$  The required A.P is

$$1, 1 + \frac{1}{7}, 1 + \frac{2}{7}, 1 + \frac{3}{7}, \dots, +\infty$$

$$\text{or } 1, \frac{8}{7}, \frac{9}{7}, \frac{10}{7}, \frac{11}{7}, \dots, \infty$$

#### Arithmetic Progressions Ex 19.4 Q18

Given,

$$a_3 = 7 = a + 2d \quad \text{---(i)}$$

$$a_7 = 3a_3 + 2$$

$$\therefore a_7 = 3(7) + 2 \quad [\because a_3 = 7]$$

$$= 23 = a + 6d \quad \text{---(ii)}$$

solving (i) and (ii)

$$a = -1, d = 4$$

Then, sum of 20 terms of this A.P

$$\begin{aligned} \Rightarrow S_{20} &= \frac{20}{2} [2 + (20 - 1)4] && \left[ \text{Using } S_n = \frac{n}{2} [2a + (n - 1)d] \right] \\ &= 10 \times 74 \\ &= 740 \end{aligned}$$

First term is  $-1$  common difference  $= 4$ , sum of 20 terms  $= 740$ .

#### Arithmetic Progressions Ex 19.4 Q19

Given,

$$a = 2$$

$$l = 50$$

$$\therefore l = a + (n - 1)d$$

$$50 = 2 + (n - 1)d$$

$$(n - 1)d = 48 \quad \text{---(i)}$$

$S_n$  of all  $n$  terms is given 442

$$\therefore S_n = \frac{n}{2} [a + l]$$

$$442 = \frac{n}{2} [2 + 50]$$

$$\text{or } n = 17 \quad \text{---(ii)}$$

From (i) and (ii)

$$d = \frac{48}{n - 1} = \frac{48}{16} = 3$$

The common difference is 3.

#### Arithmetic Progressions Ex 19.4 Q20

Let no. of terms be  $2n$

$$\text{Odd terms sum} = 24 = T_1 + T_3 + \dots + T_{2n-1}$$

$$\text{Even terms sum} = 30 = T_2 + T_4 + \dots + T_{2n}$$

Subtract above two equations

$$nd = 6$$

$$T_{2n} = T_1 + \frac{21}{2}$$

$$T_{2n} - a = \frac{21}{2}$$

$$(2n-1)d = \frac{21}{2}$$

$$12 - \frac{21}{2} = d = \frac{3}{2}$$

$$\Rightarrow n = 6 \times \frac{2}{3} = 4$$

$$\text{Total terms} = 2n = 8$$

Substitute above values in equation of sum of even terms or odd terms, we get

$$a = \frac{3}{2}$$

So series is  $\frac{3}{2}, 3, \frac{9}{2}, \dots$

**Arithmetic Progressions Ex 19.4 Q21**

Let  $a$  be the first term of the AP and  $d$  is the common difference. Then

$$S_n = \frac{n}{2}(2a + (n-1)d)$$

$$n^2 p = \frac{n}{2}(2a + (n-1)d)$$

$$np = \frac{1}{2}[2a + (n-1)d]$$

$$2np = 2a + (n-1)d \quad \dots\dots(1)$$

Again

$$S_m = \frac{m}{2}(2a + (m-1)d)$$

$$m^2 p = \frac{m}{2}(2a + (m-1)d)$$

$$mp = \frac{1}{2}[2a + (m-1)d]$$

$$2mp = 2a + (m-1)d \quad \dots\dots(2)$$

Now subtract (1) from (2)

$$2p(m-n) = (m-n)d$$

$$d = 2p$$

Therefore

$$2mp = 2a + (m-1) \cdot 2p$$

$$2a = 2p$$

$$a = p$$

The sum up to  $p$  terms will be:

$$S_p = \frac{p}{2}(2a + (p-1)d)$$

$$= \frac{p}{2}(2p + (p-1) \cdot 2p)$$

$$= \frac{p}{2}(2p + 2p^2 - 2p)$$

$$= p^3$$

Hence it is shown.

#### Arithmetic Progressions Ex 19.4 Q22

$$a_{12} = a + 11d = -13 \quad \text{---(i)} \quad \text{[Given]}$$

$$s_4 = \frac{4}{2}(2a + 3d) = 24 \quad \text{---(ii)} \quad \text{[Given]}$$

From (i) and (ii)

$$d = -2 \text{ and } a = 9$$

Then,

Sum of first 10 terms is

$$s_{10} = \frac{10}{2}[2 \times 9 + (9)(-2)]$$

$$= 0$$

$$\left[ \text{Using } S_n = \frac{n}{2}[2a + (n-1)d] \right]$$

Sum of first 10 terms is zero.

#### Arithmetic Progressions Ex 19.4 Q23

$$a_5 = a + 4d = 30 \quad \text{---(i)} \quad [\text{Given}]$$

$$a_{12} = a + 11d = 65 \quad \text{---(ii)} \quad [\text{Given}]$$

From (i) and (ii)

$$d = 5 \text{ and } a = 10$$

Then,

Sum of first 20 terms is

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\begin{aligned} \Rightarrow S_{20} &= \frac{20}{2} [2 \times 10 + (20-1)5] \\ &= 1150 \end{aligned}$$

Sum of first 20 terms is 1150.

#### Arithmetic Progressions Ex 19.4 Q24

Here,

$$a_k = 5k + 1$$

$$a_1 = 5 + 1 = 6$$

$$a_2 = 5(2) + 1 = 11$$

$$a_3 = 5(3) + 1 = 16$$

$$d = 11 - 6 = 16 - 11 = 5$$

$$\begin{aligned} S_n &= \frac{n}{2} [2a + (n-1)d] \\ &= \frac{n}{2} [2(6) + (n-1)(5)] \\ &= \frac{n}{2} [12 + 5n - 5] \\ S_n &= \frac{n}{2} (5n + 7) \end{aligned}$$

#### Arithmetic Progressions Ex 19.4 Q25

sum of all two digit numbers which when divided by 4,

yields 1 as remainder,  $\Rightarrow$  all  $4n+1$  terms with  $n \geq 3$

13,17,21,.....97

$$n = 22, a = 13, d = 4$$

$$\text{sum of terms} = \frac{22}{2} [26 + 21 \times 4] = 11 \times 110 = 1210$$

#### Arithmetic Progressions Ex 19.4 Q26

Sum of terms 25, 22, 19,....., is 116

$$\frac{n}{2}[50 + (n-1)(-3)] = 116$$

$$\frac{n}{2}[53 - 3n] = 116$$

$$53n - 3n^2 = 232$$

$$3n^2 - 53n + 232 = 0$$

$$3n^2 - 29n - 24n + 232 = 0$$

$$n(3n - 29) - 8(3n - 29) = 0$$

$$(3n - 29)(n - 8) = 0$$

$$\Rightarrow n = 8 \text{ or } \frac{29}{3}$$

n cannot be in fraction, so n=8

$$\text{last term} = 25 - 7 \times 3 = 4$$

### Arithmetic Progressions Ex 19.4 Q27

Let the number of terms is  $n$ .

Now the sum of the series is:

$$1 + 3 + 5 + \dots + 2001$$

Here  $l = 2001$  and  $d = 2$ .

Therefore

$$l = a + (n-1)d$$

$$2001 = 1 + (n-1) \cdot 2$$

$$2(n-1) = 2000$$

$$n-1 = 1000$$

$$n = 1001$$

Therefore the sum of the series is:

$$S = \frac{1001}{2} [2 + (1001-1)2]$$

$$= 1001^2$$

$$= 1002001$$

### Arithmetic Progressions Ex 19.4 Q28

Let the number of terms to be added to the series is  $n$ .

Now  $a = -6$  and  $d = 0.5$ .

Therefore

$$-25 = \frac{n}{2} [2(-6) + (n-1)(0.5)]$$

$$-50 = n[-12 + 0.5n - 0.5]$$

$$-12.5n + 0.5n^2 + 50 = 0$$

$$n^2 - 25n + 100 = 0$$

$$n = 20, 5$$

Therefore the value of  $n$  will be either 20 or 5.

### Arithmetic Progressions Ex 19.4 Q29

Here the first term  $a = 2$ . Let the common difference is  $d$ .

Now

$$\frac{5}{2}[2a + (5-1)d] = \frac{1}{4}\left[\frac{5}{2}[2(a+5d) + (5-1)d]\right]$$

$$\frac{5}{2}[2 \cdot 2 + 4d] = \frac{5}{8}[2 \cdot 2 + 14d]$$

$$10 + 10d = \frac{5}{2} + \frac{35}{4}d$$

$$\frac{5}{4}d = -7.5$$

$$d = -6$$

The 20<sup>th</sup> term will be:

$$\begin{aligned} a + (n-1)d &= 2 + (20-1)(-6) \\ &= -112 \end{aligned}$$

Hence it is shown.

#### Arithmetic Progressions Ex 19.4 Q30

$$S_{(2n+1)} = S_1 = \frac{(2n+1)}{2}[2a + (2n+1-1)d]$$

$$S_1 = \frac{(2n+1)}{2}[2a + 2nd]$$

$$= (2n+1)(a + nd)$$

--- (i)

Sum of odd terms  $s = S_2$

$$S_2 = \frac{(n+1)}{2}[2a + (n+1-1)(2d)]$$

$$= \frac{(n+1)}{2}[2a + 2nd]$$

$$S_2 = (n+1)(a + nd)$$

--- (ii)

From equation (i) and (ii),

$$S_1 : S_2 = (2n+1)(a + nd) : (n+1)(a + nd)$$

$$S_1 : S_2 = (2n+1) : (n+1)$$

#### Arithmetic Progressions Ex 19.4 Q31



Here,

$$S_n = 3n^2 \quad \text{---(i)} \quad \text{[Given]}$$

Where  $n$  is number of term

$$\therefore S_n = \frac{n}{2}[2a + (n-1)d] \quad \text{---(ii)}$$

From (i) and (ii)

$$3n^2 = \frac{n}{2}[2a + (n-1)d]$$

$$6n = 2a + nd - d$$

Equating both sides

$$6n = nd$$

$$\therefore d = 6 \quad \text{---(iii)}$$

and

$$0 = 2a - d$$

$$\text{or } d = 2a \quad \text{---(iv)}$$

From (iii) and (iv)

$$a = 3 \text{ and } d = 6$$

$\therefore$  The required A.P is  $3, 9, 15, 21, \dots, \infty$

### Arithmetic Progressions Ex 19.4 Q32

$$S_n = nP + \frac{1}{2}n(n-1)Q \quad \text{[Given]}$$

$$S_n = \frac{n}{2}[2P + (n-1)Q] \quad \text{---(i)}$$

We know

$$S_n = \frac{n}{2}[2a + (n-1)d] \quad \text{---(ii)}$$

Where  $a$  = first term and  $d$  = common difference comparing (i) and (ii)

$$d = Q$$

$\therefore$  The common difference is  $Q$ .

### Arithmetic Progressions Ex 19.4 Q33

Let sum of  $n$  terms of two A.P be  $S_n$  and  $S'_n$ .

Then,  $S_n = 5n + 4$  and  $S'_n = 9n + 16$  respectively.

Then, if ratio of sum of  $n$  terms of 2A.P is given, then the ratio of their  $n$ th term is obtained by replacing  $n$  by  $(2n - 1)$ .

$$\frac{a_n}{a'_n} = \frac{5(2n - 1) + 4}{9(2n - 1) + 16}$$

∴ Ratio of their 18th term is

$$\begin{aligned}\frac{a_{18}}{a'_{18}} &= \frac{5(2 \times 18 - 1) + 4}{9(2 \times 18 - 1) + 16} \\ &= \frac{5 \times 35 + 4}{9 \times 35 + 16} \\ &= \frac{179}{321}\end{aligned}$$

#### Arithmetic Progressions Ex 19.4 Q34

Let sum of  $n$  terms of 1 A.P series be  $S_n$  and other  $S'_n$

The,  $S_n = 7n + 2$  --- (i).

$S'_n = n + 4$  --- (ii)

If the ratio of sum of  $n$  terms of 2 A.P is given, then the ratio of their  $n$ th term is obtained by replacing  $n$  by  $(2n - 1)$ .

$$\frac{a_n}{a'_n} = \frac{7(2n - 1) + 2}{(2n - 1) + 4}$$

Putting  $n = 5$  to get the ratio of 5th term, we get

$$\frac{a_5}{a'_5} = \frac{7(2 \times 5 - 1) + 2}{(2 \times 5 - 1) + 4} = \frac{65}{13} = \frac{5}{1}$$

The ratio is 5 : 1.