Exercise -1.3

1.

Sol:

Let
$$x = 0 \cdot \overline{4}$$

Now,
$$x = 0.\overline{4} = 0.444...$$

Multiplying both sides of equation (1) by 10, we get, y 1(2)

$$10x = 4.444$$

Subtracting equation (1) by (2)

$$\therefore 10x - x = 4.444... - 0.444...$$

$$\Rightarrow 9x = 4$$

$$\Rightarrow x = \frac{4}{9}$$

Hence,
$$0 \cdot \overline{4} = \frac{4}{9}$$

Let
$$x = 0 \cdot \overline{37}$$

Now,
$$x = 0.3737...$$
 (1)

Multiplying equation (1) by 10.

$$\therefore 10x = 3.737$$
(2)

$$100x = 37.3737...$$
(3)

Subtracting equation (1) by equation (3)

$$\therefore 100x - x = 37$$

$$\Rightarrow$$
 99 $x = 37$

$$\Rightarrow x = \frac{37}{99}$$

Hence,
$$0.\overline{37} = \frac{37}{99}$$

2.

Sol:

(i) We have,

$$0\cdot 39 = \frac{39}{100}$$

$$\Rightarrow \boxed{0.39 = \frac{39}{100}}$$

(ii)

$$0.750 = \frac{750}{1000} = \frac{750 \div 250}{1000 \div 250} = \frac{3}{4}$$

(iii) We have

$$2.15 = \frac{215}{100} = \frac{215 \div 5}{100 \div 5} = \frac{43}{20}$$

$$\therefore 2 \cdot 15 = \frac{43}{20}$$

(iv) We have

We have,

$$0.750 = \frac{750}{1000} = \frac{750 \div 250}{1000 \div 250} = \frac{3}{4}$$
We have

$$2.15 = \frac{215}{100} = \frac{215 \div 5}{100 \div 5} = \frac{43}{20}$$

$$\therefore 2.15 = \frac{43}{20}$$
We have

$$7.010 = \frac{7010}{1000} = \frac{7010 \div 10}{1000 \div 10} = \frac{701}{100}$$

$$\therefore 7010 = \frac{701}{100}$$
We have,

$$90 = \frac{990}{100} = \frac{990 \div 10}{100 \div 10} = \frac{99}{10}$$

$$\therefore 7010 = \frac{701}{100}$$

(v)

$$9 \cdot 90 = \frac{990}{100} = \frac{990 \div 10}{100 \div 10} = \frac{99}{10}$$

$$\therefore 9.90 = \frac{99}{10}$$

(vi) We have,

$$1 \cdot 0001 = \frac{10001}{10000}$$

$$\therefore \boxed{1.0001 = \frac{10001}{10000}}$$