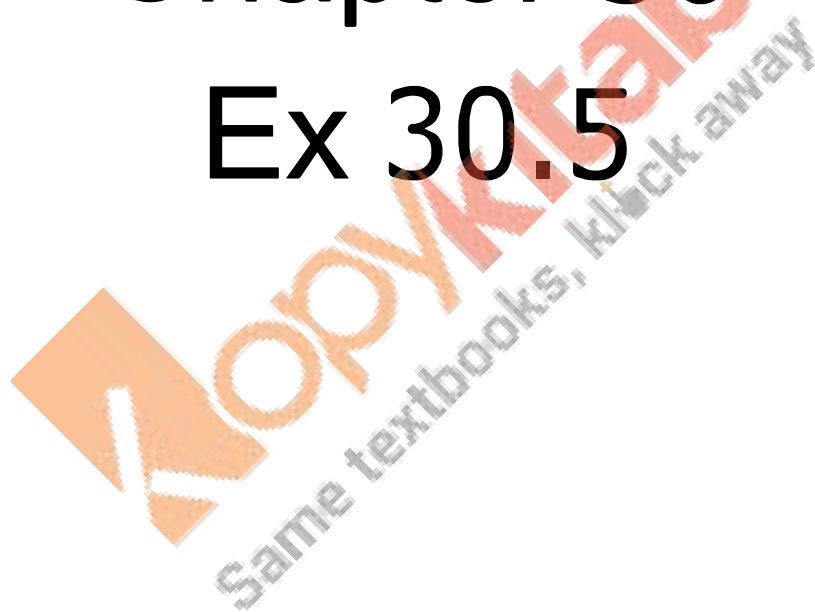


RD Sharma
Solutions
Class 11 Maths
Chapter 30
Ex 30.5



Derivatives Ex 30.5 Q1

Using quotient rule, we have

$$\begin{aligned}\frac{d}{dx} \left(\frac{x^2+1}{x+1} \right) &= \frac{(x+1) \frac{d}{dx} (x^2+1) - (x^2+1) \frac{d}{dx} (x+1)}{(x+1)^2} \\ &= \frac{(x+1) \times 2x - (x^2+1) \times 1}{(x+1)^2} \\ &= \frac{2x^2+2x-x^2-1}{(x+1)^2} \\ &= \frac{x^2+2x-1}{(x+1)^2}\end{aligned}$$

Derivatives Ex 30.5 Q2

Using quotient rule, we have get,

$$\begin{aligned}\frac{d}{dx} \left(\frac{2x-1}{x^2+1} \right) &= \frac{(x^2+1) \frac{d}{dx} (2x-1) - (2x-1) \frac{d}{dx} (x^2+1)}{(x^2+1)^2} \\ &= \frac{(x^2+1) \times 2 - (2x-1) \times 2x}{(x^2+1)^2} \\ &= \frac{2x^2+2-4x^2+2x}{(x^2+1)^2} \\ &= \frac{-2x^2+2x+2}{(x^2+1)^2} \\ &= \frac{2(-x^2+x+1)}{(x^2+1)^2} \\ &= \frac{2(1+x-x^2)}{(1+x^2)^2}\end{aligned}$$

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Derivatives Ex 30.5 Q3

By using quotient rule, we have,

$$\begin{aligned} & \frac{d}{dx} \left(\frac{x + e^x}{1 + \log x} \right) \\ &= \frac{(1 + \log x) \frac{d}{dx} (x + e^x) - (x + e^x) \frac{d}{dx} (1 + \log x)}{(1 + \log x)^2} \\ &= \frac{(1 + \log x)(1 + e^x) - (x + e^x) \times \frac{d}{dx}}{(1 + \log x)^2} \\ &= \frac{x(1 + \log x + e^x + e^x \log x) - x - e^x}{x(1 + \log x)^2} \\ &= \frac{x + x \log x + xe^x + xe^x \log x - x - e^x}{x(1 + \log x)^2} \\ &= \frac{x \log x (1 + e^x) - e^x (1 - x)}{x(1 + \log x)^2} \end{aligned}$$

Derivatives Ex 30.5 Q4

Using quotient rule, we have,

$$\begin{aligned} & \frac{d}{dx} \left(\frac{e^x - \tan x}{\cot x - x^n} \right) \\ &= \frac{(\cot x - x^n) \frac{d}{dx} (e^x - \tan x) - (e^x - \tan x) \frac{d}{dx} (\cot x - x^n)}{(\cot x - x^n)^2} \\ &= \frac{(\cot x - x^n)(e^x - \sec^2 x) - (e^x - \tan x)(-\operatorname{cosec}^2 x - nx^{n-1})}{(\cot x - x^n)^2} \\ &= \frac{(\cot x - x^n)(e^x - \sec^2 x) + (e^x - \tan x)(\operatorname{cosec}^2 x + nx^{n-1})}{(\cot x - x^n)^2} \end{aligned}$$

Derivatives Ex 30.5 Q5

Using quotient rule, we have,

$$\begin{aligned} & \frac{d}{dx} \left(\frac{ax^2 + bx + c}{px^2 + qx + r} \right) \\ &= \frac{(px^2 + qx + r) \frac{d}{dx} (ax^2 + bx + c) - (ax^2 + bx + c) \frac{d}{dx} (px^2 + qx + r)}{(px^2 + qx + r)^2} \\ &= \frac{(px^2 + qx + r)(2ax + b) - (ax^2 + bx + c)(2px + q)}{(px^2 + qx + r)^2} \\ &= \frac{2apx^3 + 2aqx^2 + 2axr + bpx^2 + bqx + br - (2apx^3 + 2pbx^2 + 2pcx + qax^2 + bqx + cq)}{(px^2 + qx + r)^2} \\ &= \frac{2apx^3 - 2apx^3 + 2aqx^2 + bpx^2 - 2pbx^2 - qax^2 + 2arx + bqx - 2pcx - bqx + br - cq}{(px^2 + qx + r)^2} \\ &= \frac{aqx^2 - bpx^2 + 2arx - 2pcx + br - cq}{(px^2 + qx + r)^2} \\ &= \frac{x^2(aq - bp) + 2(ar - cp)x + br - cq}{(px^2 + qx + r)^2} \\ &= \frac{(aq - bp)x^2 + 2(ar - cp)x + br - cq}{(px^2 + qx + r)^2} \end{aligned}$$

Derivatives Ex 30.5 Q6

Using quotient rule, we have,

$$\begin{aligned} & \frac{d}{dx} \left(\frac{x}{1 + \tan x} \right) \\ &= \frac{(1 + \tan x) \frac{d}{dx} (x) - x \frac{d}{dx} (1 + \tan x)}{(1 + \tan x)^2} \\ &= \frac{(1 + \tan x) - x(\sec^2 x)}{(1 + \tan x)^2} \end{aligned}$$

$$= \frac{1 + \tan x - x \sec^2 x}{(1 + \tan x)^2}$$

Derivatives Ex 30.5 Q7

Using quotient rule, we have

$$\begin{aligned} & \frac{d}{dx} \left(\frac{1}{ax^2 + bx + c} \right) \\ &= \frac{(ax^2 + bx + c) \frac{d}{dx}(1) - 1 \times \frac{d}{dx}(ax^2 + bx + c)}{(ax^2 + bx + c)^2} \\ &= \frac{-(2ax + b)}{(ax^2 + bx + c)^2} \\ \therefore \frac{d}{dx} \frac{1}{ax^2 + bx + c} &= \frac{-(2ax + b)}{(ax^2 + bx + c)^2} \end{aligned}$$

Derivatives Ex 30.5 Q8

We have,

$$\frac{d}{dx} \left(\frac{e^x}{1+x^2} \right)$$

Using quotient rule,

$$\begin{aligned} &= \frac{(1+x^2) \frac{d}{dx}(e^x) - (e^x) \frac{d}{dx}(1+x^2)}{(1+x^2)^2} \\ &= \frac{(1+x^2)e^x - e^x \times 2x}{(1+x^2)^2} \\ &= \frac{e^x(1+x^2-2x)}{(1+x^2)^2} \end{aligned}$$

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$$= \frac{e^x (1-x)^2}{(1+x^2)^2}$$

Derivatives Ex 30.5 Q9

We have,

$$\frac{d}{dx} \left(\frac{e^x + \sin x}{1 + \log x} \right)$$

Using quotient rule, we get

$$\begin{aligned} &= \frac{(1 + \log x) \frac{d}{dx} (e^x + \sin x) - (e^x + \sin x) \frac{d}{dx} (1 + \log x)}{(1 + \log x)^2} \\ &= \frac{(1 + \log x)(e^x + \cos x) - (e^x + \sin x) \frac{1}{x}}{(1 + \log x)^2} \\ &= \frac{x(1 + \log x)(e^x + \cos x) - (e^x + \sin x)}{x(1 + \log x)^2} \end{aligned}$$

Derivatives Ex 30.5 Q10

We have,

$$\frac{d}{dx} \left(\frac{x \tan x}{\sec x + \tan x} \right)$$

Using quotient rule, we get

$$\begin{aligned} &= \frac{(\sec x + \tan x) \frac{d}{dx} (x \tan x) - (x \tan x) \frac{d}{dx} (\sec x + \tan x)}{(\sec x + \tan x)^2} \\ &= \frac{(\sec x + \tan x)(x \sec^2 x + \tan x) - (x \tan x)(\sec x \tan x + \sec^2 x)}{(\sec x + \tan x)^2} \quad [\text{Used product rule}] \\ &= \frac{(\sec x + \tan x)(x \sec^2 x + \tan x) - x \sec x + \tan^2 x - x \tan x \sec^2 x}{(\sec x + \tan x)^2} \\ &= \frac{(\sec x + \tan x)(x \sec^2 x + \tan x) - x \tan x (\sec x \tan x + \sec^2 x)}{(\sec x + \tan x)^2} \\ &= \frac{(\sec x + \tan x)(x \sec^2 x + \tan x) - x \tan x \sec x (\sec x + \tan x)}{(\sec x + \tan x)^2} \\ &= \frac{(x \sec^2 x + \tan x - x \tan x \sec x)(\sec x + \tan x)}{(\sec x + \tan x)^2} \\ &= \frac{(x \sec^2 x + \tan x - x \tan x \sec x)}{(\sec x + \tan x)} \\ &= \frac{x \sec x (\sec x - \tan x) + \tan x}{(\sec x + \tan x)} \end{aligned}$$