EXERCISE 11.2

PAGE NO: 246

In each of the following Exercises 1 to 6, find the coordinates of the focus, axis of the parabola, the equation of the directrix and the length of the latus rectum.

1. $v^2 = 12x$ **Solution:** Given: The equation is $y^2 = 12x$ Here we know that the coefficient of x is positive. So, the parabola opens towards the right. On comparing this equation with $y^2 = 4ax$, we get, 4a = 12 a = 3 Thus, the co-ordinates of the focus = (a, 0) = (3, 0)ooliss his chart Since, the given equation involves y^2 , the axis of the parabola is the x-axis. \therefore The equation of directrix, x = -a, then, x + 3 = 0Length of latus rectum = $4a = 4 \times 3 = 12$ 2. $x^2 = 6y$ Solution: Given: The equation is $x^2 = 6y$ Here we know that the coefficient of y is positive. So, the parabola opens upwards. On comparing this equation with $x^2 = 4ay$, we get, 4a = 6a = 6/4= 3/2

Thus, the co-ordinates of the focus = (0, a) = (0, 3/2)Since, the given equation involves x^2 , the axis of the parabola is the y-axis. \therefore The equation of directrix, y =-a, then, y = -3/2Length of latus rectum = 4a = 4(3/2) = 6

3. $y^2 = -8x$ Solution: Given: The equation is $y^2 = -8x$ Here we know that the coefficient of x is negative. So, the parabola open towards the left. On comparing this equation with $y^2 = -4ax$, we get, -4a = -8a = -8/-4 = 2Thus, co-ordinates of the focus = (-a,0) = (-2, 0)Since, the given equation involves y^2 , the axis of the parabola is the x-axis. \therefore Equation of directrix, x =a, then, $\mathbf{x} = 2$ Length of latus rectum = 4a = 4(2) = 8

4. $x^2 = -16y$ Solution:

Given:

So, the parabola opens downwards. On comparing this equation with $x^2 = -4ay$, we get, -4a = -16a = -16/-4= 4Thus, co-ordinates of the focus = (0, -a) = (0, -4)Since, the given equation involves 2 Since, the given equation involves x^2 , the axis of the parabola is the y-axis.

 \therefore The equation of directrix, y =a, then,

 $\mathbf{v} = 4$

Length of latus rectum = 4a = 4(4) = 16

5. $y^2 = 10x$

Solution:

Given: The equation is $y^2 = 10x$ Here we know that the coefficient of x is positive. So, the parabola open towards the right. On comparing this equation with $y^2 = 4ax$, we get, 4a = 10 a = 10/4 = 5/2Thus, co-ordinates of the focus = (a,0) = (5/2, 0)

Since, the given equation involves y^2 , the axis of the parabola is the x-axis. \therefore The equation of directrix, x =-a, then, x = -5/2Length of latus rectum = 4a = 4(5/2) = 10

6. $x^2 = -9y$ Solution:

Given: The equation is $x^2 = -9y$ Here we know that the coefficient of y is negative. So, the parabola open downwards. On comparing this equation with $x^2 = -4ay$, we get, -4a = -9a = -9/-4 = 9/4Thus, co-ordinates of the focus = (0, -a) = (0, -9/4)Since, the given equation involves x^2 , the axis of the parabola is the y-axis. TCH anna \therefore The equation of directrix, y = a, then, y = 9/4Length of latus rectum = 4a = 4(9/4) = 9

In each of the Exercises 7 to 12, find the equation of the parabola that satisfies the extbook5 given conditions:

7. Focus (6,0); directrix x = -6Solution:

Given:

Focus (6,0) and directrix x = -6

We know that the focus lies on the x-axis is the axis of the parabola.

So, the equation of the parabola is either of the form $y^2 = 4ax$ or $y^2 = -4ax$.

It is also seen that the directrix, x = -6 is to the left of the y- axis,

While the focus (6, 0) is to the right of the y –axis.

Hence, the parabola is of the form $y^2 = 4ax$.

Here, a = 6

: The equation of the parabola is $y^2 = 24x$.

8. Focus (0,-3); directrix y = 3 Solution:

Given: Focus (0, -3) and directrix y = 3

We know that the focus lies on the y-axis, the y-axis is the axis of the parabola. So, the equation of the parabola is either of the form $x^2 = 4ay$ or $x^2 = -4ay$. It is also seen that the directrix, y = 3 is above the x- axis, While the focus (0,-3) is below the x-axis. Hence, the parabola is of the form $x^2 = -4ay$. Here, a = 3: The equation of the parabola is $x^2 = -12y$.

9. Vertex (0, 0); focus (3, 0)

Solution:

Given:

Vertex (0, 0) and focus (3, 0)

We know that the vertex of the parabola is (0, 0) and the focus lies on the positive x-axis. [x-axis is the axis of the parabola.]

The equation of the parabola is of the form $y^2 = 4ax$.

Since, the focus is (3, 0), a = 3

: The equation of the parabola is $y^2 = 4 \times 3 \times x$,

$$y^2 = 12x$$

10. Vertex (0, 0); focus (-2, 0) Solution:

Given:

Vertex (0, 0) and focus (-2, 0)

H.S. Markaway We know that the vertex of the parabola is (0, 0) and the focus lies on the positive x-axis. [x-axis is the axis of the parabola.]

The equation of the parabola is of the form y^2 =-4ax.

Since, the focus is (-2, 0), a = 2

: The equation of the parabola is $y^2 = -4 \times 2 \times x$, $v^2 = -8x$

11. Vertex (0, 0) passing through (2, 3) and axis is along x-axis. Solution:

We know that the vertex is (0, 0) and the axis of the parabola is the x-axis

The equation of the parabola is either of the from $y^2 = 4ax$ or $y^2 = -4ax$.

Given that the parabola passes through point (2, 3), which lies in the first quadrant.

So, the equation of the parabola is of the form $y^2 = 4ax$, while point (2, 3) must satisfy the equation $y^2 = 4ax$.

Then,

 $3^2 = 4a(2)$

 $3^2 = 8a$ 9 = 8aa = 9/8Thus, the equation of the parabola is $y^2 = 4 (9/8)x$ = 9x/2 $2v^2 = 9x$ \therefore The equation of the parabola is $2y^2 = 9x$

12. Vertex (0, 0), passing through (5, 2) and symmetric with respect to y-axis. Solution:

We know that the vertex is (0, 0) and the parabola is symmetric about the y-axis.

The equation of the parabola is either of the from $x^2 = 4ay$ or $x^2 = -4ay$.

Given that the parabola passes through point (5, 2), which lies in the first quadrant.

So, the equation of the parabola is of the form $x^2 = 4ay$, while point (5, 2) must satisfy the Just the parabola is -25y/2 $2x^2 = 25y$ \therefore The equation of the parabola is $2x^2 = 25y$ equation $x^2 = 4ay$.