Direct and Inverse Proportions

Ex 12A

Q1.

Answer:

(i)

Clearly, $\frac{x}{y} = \frac{3}{9} = \frac{5}{15} = \frac{8}{24} = \frac{11}{33} = \frac{26}{78} = \frac{1}{3}$ (constant)

Therefore, x and y are proportional.

(ii) Clearly, $\frac{x}{y} = \frac{2.5}{10} = \frac{4}{16} = \frac{7.5}{30} = \frac{10}{40} = \frac{1}{4}$, while $\frac{14}{42} = \frac{1}{3}$ i.e., $\frac{2.5}{10} = \frac{4}{16} = \frac{7.5}{30} = \frac{10}{40}$ is not equal to $\frac{14}{42}$. Therefore, x and y are not proportional.

(iii) Clearly, $\frac{x}{y} = \frac{5}{15} = \frac{7}{21} = \frac{9}{27} = \frac{25}{75} = \frac{1}{3}$, while $\frac{15}{60} = \frac{18}{72} = \frac{1}{4}$ i.e., $\frac{5}{15} = \frac{7}{21} = \frac{9}{27} = \frac{25}{75}$ is not equal to $\frac{15}{60}$ and $\frac{18}{72}$. Therefore, x and y are not proportional.

Q2.

Answer:

Since x and y are directly proportional, we have:

$$\frac{\frac{3}{72} = \frac{x_1}{120} = \frac{x_2}{192} = \frac{10}{y_1}}{\text{Now, } \frac{3}{72} = \frac{x_1}{120}}$$

$$\Rightarrow x_1 = \frac{120 \times 3}{72} = 5$$

And,
$$\frac{3}{72} = \frac{x_2}{192}$$

 $\Rightarrow x_2 = \frac{3 \times 192}{72} = 8$
And, $\frac{3}{72} = \frac{10}{y_1}$
 $\Rightarrow y_1 = \frac{72 \times 10}{3} = 240$
Therefore, $x_1 = 5$, $x_2 = 8$ and $y_1 = 240$

Q3.

Let the required distance be x km. Then, we have:

Quantity of diesel (in litres)	34	20
Distance (in km)	510	X

Clearly, the less the quantity of diesel consumed, the less is the distance covered. So, this is a case of direct proportion.

Now,
$$\frac{34}{510} = \frac{20}{x}$$

 $\Rightarrow \frac{1}{15} = \frac{20}{x}$
 $\Rightarrow x \times 1 = 20 \times 15 = 300$

Therefore, the required distance is 300 km.

Q4.

Answer:

Let the required charge be Rs x. Then, we have:

Distance (in km)	150	124
Taxi charges (in rupees	1275	\boldsymbol{x}

Clearly, the less the distance covered, the less will be the taxi charges.

So, this is a case of direct proportion.

Now,
$$\frac{150}{1275} = \frac{124}{x}$$

 $\Rightarrow \frac{2}{17} = \frac{124}{x}$
 $\Rightarrow (2 \times x) = (124 \times 17)$
 $\Rightarrow x = \frac{124 \times 17}{2}$
 $\Rightarrow x = 62 \times 17 = 1054$

Therefore, the required charge is Rs 1,054.

Q5.

Answer:

Let the required distance be x km. Then, we have:

$$1 h = 60 min$$

$$\begin{tabular}{lll} \textbf{i.e., } 5 \textbf{ h} = 5 \times 60 = 300 \mbox{ min} \\ \hline \mbox{Distance (in km)} & 16 \mbox{ } x \\ \hline \mbox{Time (in min)} & 25 \mbox{ } 300 \\ \hline \end{tabular}$$

Clearly, the more the time taken, the more will be the distance covered.

So, this is a case of direct proportion.

Now,
$$\frac{16}{25} = \frac{x}{300}$$

 $\Rightarrow x = \left(\frac{16 \times 300}{25}\right)$
 $\Rightarrow x = 192$

Therefore, the required distance is 192 km.

Q6.

Answer:

Let the required number of dolls be x. Then, we have:

No of dolls	18	X
Cost of dolls (in rupees)	630	455

Clearly, the less the amount of money, the less will be the number of dolls bought. So, this is a case of direct proportion. Now, $\frac{18}{630}=\frac{x}{455}$

Now,
$$\frac{18}{630} = \frac{x}{450}$$

$$\Rightarrow \frac{1}{35} = \frac{x}{450}$$

$$\Rightarrow x = \frac{455}{35}$$

$$\Rightarrow x = 13$$

Therefore, 13 dolls can be bought for Rs 455.

Let the required weight of sugar be x kg. Then, we have:

Weight of sugar (in kg)	9	X
Cost of sugar (in rupees)	166.50	259

Clearly, more quantity of sugar can be bought for more amount of money.

So, this is a case of direct proportion.

Now,
$$\frac{9}{166.50} = \frac{x}{259}$$

 $\Rightarrow x = \frac{9 \times 259}{166.50}$
 $\Rightarrow x = \frac{9 \times 259 \times 100}{16650}$
 $\Rightarrow x = 14$

Therefore, 14 kg of sugar can be bought for Rs 259.

Q8.

Answer:

Let the length of cloth be x m. Then, we have:

Length of cloth (in metres)	15	x
Cost of cloth (in rupees)	981	1308

Clearly, more length of cloth can be bought by more amount of money.

So, this is a case of direct proportion.

Now,
$$\frac{15}{981} = \frac{x}{1308}$$

 $\Rightarrow x = \frac{15 \times 1308}{981}$
 $\Rightarrow x = 20$

Therefore, 20 m of cloth can be bought for Rs 1,308.

Q9.

Answer:

Let x m be the length of the model of the ship. Then, we have:

$$1 \text{ m} = 100 \text{ cm}$$

Therefore, $15 \text{ m} = 1500 \text{ cm}$
 $35 \text{ m} = 3500 \text{ cm}$

	Length of the mast (in cm)	Length of the ship (in cm)
Actual ship	1500	3500
Model of the ship	9	x

Clearly, if the length of the actual ship is more, then the length of the model ship will also be more. So, this is a case of direct proportion.

Now,
$$\frac{1500}{9} = \frac{3500}{x}$$

 $\Rightarrow x = \frac{3500 \times 9}{1500}$
 $\Rightarrow x = 21 \text{ cm}$

Therefore, the length of the model of the ship is 21 cm.

Q10.

Let x kg be the required amount of dust. Then, we have:

No. of days	8	15
Dust (in kg)	6.4 × 10 ⁷	Х

Clearly, more amount of dust will be collected in more number of days. So, this is a case of direct proportion.

Now,
$$\frac{8}{6.4 \times 10^7} = \frac{15}{x}$$

 $\Rightarrow x = \frac{15 \times 6.4 \times 10^7}{8}$
 $\Rightarrow x = 12 \times 10^7$

Therefore, 12,00,00,000 kg of dust will be picked up in 15 days.

Q11.

Answer:

Let x km be the required distance. Then, we have:

$$1 h = 60 min$$

i.e., $1h 12 min = (60 + 12) min = 72 min$

Distance covered (in km)	50	х
Time (in min)	60	72

Clearly, more distance will be covered in more time.

So, this is a case of direct proportion.

Now,
$$\frac{50}{60} = \frac{x}{72}$$

 $\Rightarrow x = \frac{50 \times 72}{60}$
 $\Rightarrow x = 60$

Therefore, the distance travelled by the car in 1 h 12 min is 60 km.

Q12.

Answer:

Let x km be the required distance covered by Ravi in 2 h 24 min.

Then, we have:

$$1 h = 60 \min$$

i.e., $2 h 24 \min = (120 + 24) \min = 144 \min$

Distance covered (in km)	5	Х
Time (in min)	60	144

Clearly, more distance will be covered in more time.

So, this is a case of direct proportion.

Now,
$$\frac{5}{60} = \frac{x}{144}$$

 $\Rightarrow x = \frac{5 \times 144}{60}$
 $\Rightarrow x = 12$

Therefore, the distance covered by Ravi in 2 h 24 min is 12 km.

Q13.

Let x mm be the required thickness. Then, we have:

Thickness of cardboard (in mm)	65	X
No. of cardboards	12	312

Clearly, when the number of cardboard is more, the thickness will also be more. So, it is a case of direct proportion.

Now,
$$\frac{65}{12} = \frac{x}{312}$$

 $\Rightarrow x = \frac{65 \times 312}{12}$
 $\Rightarrow x = 1690$

Therefore, the thickness of the pile of 312 cardboards is 1690 mm.

Q14.

Answer:

Let x be the required number of men.

Now,
$$6\frac{3}{4}$$
 m = $\frac{27}{4}$ m

Then, we have:

Number of men	11	х
Length of trench (in metres)	27 4	27

Clearly, the longer the trench, the greater will be the number of men required. So, it is a case of direct proportion.

Now,
$$\frac{11}{\frac{27}{4}} = \frac{x}{27}$$

$$\Rightarrow \frac{11 \times 4}{27} = \frac{x}{27}$$

$$\Rightarrow x = 44$$

Therefore, 44 men should be employed to dig a trench of length 27 m.

Q15.

Answer:

Let Reenu type x words in 8 minutes.

No. of words	540	Х
Time taken (in min)	30	8

Clearly, less number of words will be typed in less time.

So, it is a case of direct proportion.

So, it is a case of Now,
$$\frac{540}{30} = \frac{x}{8}$$

$$\Rightarrow x = \frac{540 \times 8}{30}$$

$$\Rightarrow x = 144$$

Therefore, Reenu will type 144 words in 8 minutes.