

EXERCISE – 3D

Formula Used -: $(x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$

Answer.1.

(i) $(a + 2b + 5c)^2$

$$\begin{aligned} (a + 2b + 5c)^2 &= (a)^2 + (2b)^2 + (5c)^2 + 2(a)(2b) + 2(2b)(5c) + 2(5c)(a) \\ &= a^2 + 4b^2 + 25c^2 + 4ab + 20bc + 10ac \end{aligned}$$

(ii) $(2a - b + c)^2$

$$\begin{aligned} (2a - b + c)^2 &= (2a)^2 + (-b)^2 + (c)^2 + 2(2a)(-b) + 2(-b)(c) + 2(c)(2a) \\ &= 4a^2 + b^2 + c^2 - 4ab - 2bc + 4ac \end{aligned}$$

(iii) $(a - 2b - 3c)^2$

$$\begin{aligned} (a - 2b - 3c)^2 &= (a)^2 + (-2b)^2 + (-3c)^2 + 2(a)(-2b) + 2(-2b)(-3c) + 2(-3c)(a) \\ &= a^2 + 4b^2 + 9c^2 - 4ab + 12bc - 6ac \end{aligned}$$

Answer.2.

(i) $(2a - 5b - 7c)^2$

$$\begin{aligned} (2a - 5b - 7c)^2 &= (2a)^2 + (-5b)^2 + (-7c)^2 + 2(2a)(-5b) + 2(-5b)(-7c) + 2(-7c)(2a) \\ &= 4a^2 + 25b^2 + 49c^2 - 20ab + 70bc - 28ac \end{aligned}$$

(ii) $(-3a + 4b - 5c)^2$

$$\begin{aligned} (-3a + 4b - 5c)^2 &= (-3a)^2 + (4b)^2 + (-5c)^2 + 2(-3a)(4b) + 2(4b)(-5c) + 2(-5c)(-3a) \\ &= 9a^2 + 16b^2 + 25c^2 - 24ab - 40bc + 30ac \end{aligned}$$

(iii) $\left(\frac{1}{2}a - \frac{1}{4}b + 2\right)^2$

$$\begin{aligned} \left(\frac{1}{2}a - \frac{1}{4}b + 2\right)^2 &= \left(\frac{1}{2}a\right)^2 + \left(-\frac{1}{4}b\right)^2 + (2)^2 + 2\left(\frac{1}{2}a\right)\left(-\frac{1}{4}b\right) + 2\left(-\frac{1}{4}b\right)(2) + 2(2)\left(\frac{1}{2}a\right) \\ &= \frac{a^2}{4} + \frac{b^2}{16} + 4 - \frac{ab}{4} - b + 2a \end{aligned}$$

Answer.3. $4x^2 + 9y^2 + 16z^2 + 12xy - 24yz - 16zx$

$$\begin{aligned} 4x^2 + 9y^2 + 16z^2 + 12xy - 24yz - 16zx &= (2x)^2 + (3y)^2 + (-4z)^2 + \{2(2x)(3y)\} + \\ &\quad \{2(3y)(-4z)\} + \{2(-4z)(2x)\} \\ &= \{(2x) + (3y) + (-4z)\}^2 \\ &= (2x + 3y - 4z)^2 \\ &= (2x + 3y - 4z)(2x + 3y - 4z) \end{aligned}$$

Answer.4. $9x^2 + 16y^2 + 4z^2 - 24xy + 16yz - 12zx$

$$\begin{aligned} 9x^2 + 16y^2 + 4z^2 - 24xy + 16yz - 12zx &= (-3x)^2 + (4y)^2 + (2z)^2 + \{2(-3x)(4y)\} + \\ &\quad \{2(4y)(2z)\} + \{2(2z)(-3x)\} \\ &= \{(-3x) + (4y) + (2z)\}^2 \\ &= (-3x + 4y + 2z)^2 \\ &= (-3x + 4y + 2z)(-3x + 4y + 2z) \end{aligned}$$

Answer.5. $25x^2 + 4y^2 + 9z^2 - 20xy - 12yz + 30zx$

$$\begin{aligned} 25x^2 + 4y^2 + 9z^2 - 20xy - 12yz + 30zx &= (5x)^2 + (-2y)^2 + (3z)^2 + \{2(5x)(-2y)\} + \\ &\quad \{2(-2y)(3z)\} + \{2(3z)(5x)\} \\ &= \{(5x) + (-2y) + (3z)\}^2 \\ &= (5x - 2y + 3z)^2 \\ &= (5x - 2y + 3z)(5x - 2y + 3z) \end{aligned}$$

Answer.6. $16x^2 + 4y^2 + 9z^2 - 16xy - 12yz + 24zx$

$$\begin{aligned} 16x^2 + 4y^2 + 9z^2 - 16xy - 12yz + 24zx &= (4x)^2 + (-2y)^2 + (3z)^2 + \{2(4x)(-2y)\} + \\ &\quad \{2(-2y)(3z)\} + \{2(3z)(4x)\} \\ &= \{(4x) + (-2y) + (3z)\}^2 \\ &= (4x - 2y + 3z)^2 \end{aligned}$$

$$= (4x - 2y + 3z)(4x - 2y + 3z)$$

Answer.7. (i) $(99)^2$

$$\begin{aligned}(99)^2 &= (100 - 1)^2 \\ &= (100)^2 + (1)^2 - 2 \times 100 \times 1 \\ &= 10000 + 1 - 200 \\ &= 9801\end{aligned}$$

(ii) $(995)^2$

$$\begin{aligned}(995)^2 &= (1000 - 5)^2 \\ &= (1000)^2 + (5)^2 - 2 \times 1000 \times 5 \\ &= 1000000 + 25 - 10000 \\ &= 990025\end{aligned}$$

(iii) $(107)^2$

$$\begin{aligned}(107)^2 &= (100 + 7)^2 \\ &= (100)^2 + (7)^2 + 2 \times 100 \times 7 \\ &= 10000 + 49 + 1400 \\ &= 11449\end{aligned}$$